## MATHS CLASS XII (Relations and Functions) Continuation.....

**General direction for the students** :-Whatever be the notes provided , everything must be copied in the Maths Copy and then do the Home work in the same Copy. g

## **COMPOSITION OF FUNCTIONS**

Let  $f: A \to B$  and  $g: B \to C$  be two functions, then the function from A to C is defined as  $g_0 f$  is known as composite function.

 $\Rightarrow$  gof:  $A \rightarrow C$  defined by  $gof(x) = g(f(x)), \forall x \in A.$ 

- Composition of two function is also known as Resultant of two functions or the Function of Function.
- Here Range of f must be a subset of domain of g.

## **Properties of Composition functions**

1. The composition of function is Associative

2. If f and g are one one, the gof is also one one but converse may not be true.

3. If f and g are onto, the gof is also onto but converse may not be true.

4. If  $f : A \rightarrow B$  is a function and  $I_A$ ,  $I_B$  are identity functions on A, B respectively, then

(i)  $I_B of = f$  (ii)  $f o I_A = f$ 

\*\* For the explanation above points , watch the video class. Exercise 1.4

3. Given 
$$A = \{1, 2, 3, 4\}$$
,  $f ; A \to A$ ,  $g : A \to A$   
 $f = \{(1, 4), (2, 1), (3, 3), (4, 2)\}$ ,  $g = \{(1, 3), (2, 1), (3, 2), (4, 4)\}$   
i)  $gof = \{(1, 4), (2, 3), (3, 2), (4, 1)\}$   
ii)  $fog = \{(1, 3), (2, 4), (3, 3), (4, 2)\}$   
iii)  $fof = \{(1, 2), (2, 4), (3, 3), (4, 1)\}$ 

6. Given  $f : R \to R$  defined by  $f(x) = x^2 - 3x + 2$ 

$$fof(x) = f(f(x)) = f(x^2 - 3x + 2)$$
$$= (x^2 - 3x + 2)^2 - 3(x^2 - 3x + 2) + 2$$
$$= x^6 + 6x^4 + 12x^2 + 7$$